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11. State-Space Search: Uniform Cost Search

### 11. State-Space Search: Uniform Cost Search

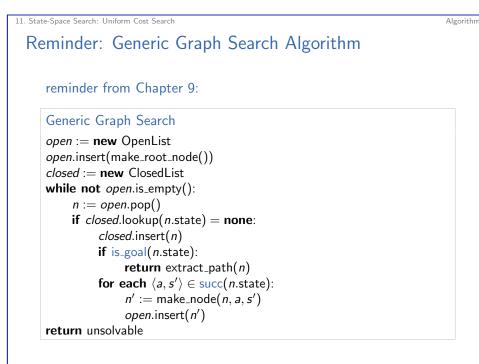
# Uniform Cost Search

- breadth-first search optimal if all action costs equal
- ▶ otherwise no optimality guarantee ~→ example:
  - consider bounded inc-and-square problem with cost(sqr) = 3
  - solution of breadth-first search still  $\langle inc, sqr, sqr \rangle$  (cost: 7)
  - **but**: (*inc*, *inc*, *inc*, *inc*) (cost: 5) is cheaper!

### remedy: uniform cost search

- always expand a node with minimal path cost (n.path\_cost a.k.a. g(n))
- implementation: priority queue (min-heap) for open list

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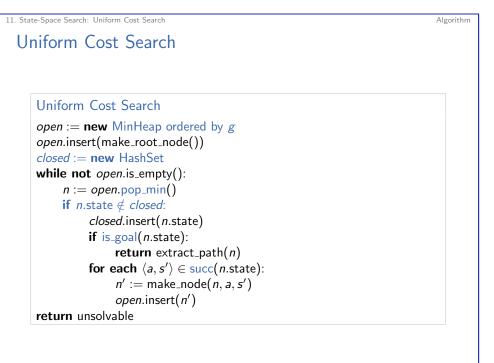
# 11.2 Algorithm

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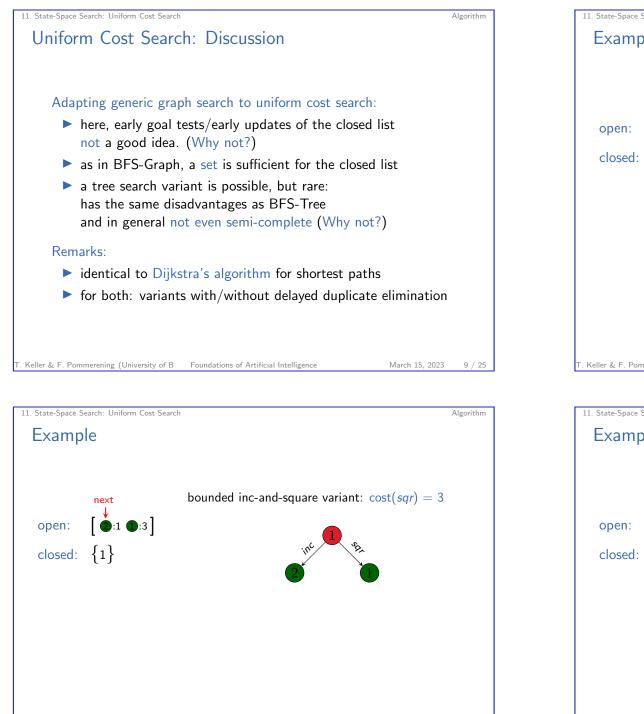
Algorithm



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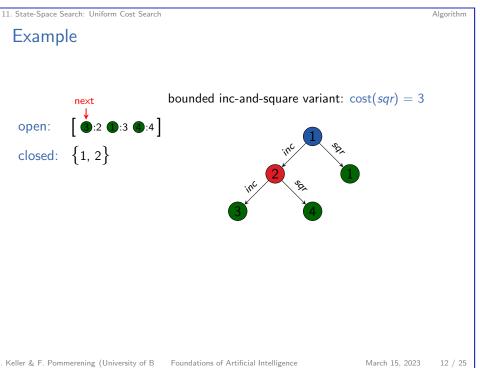
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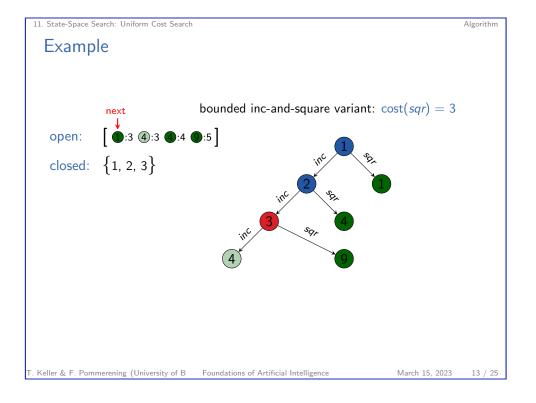
Introduction

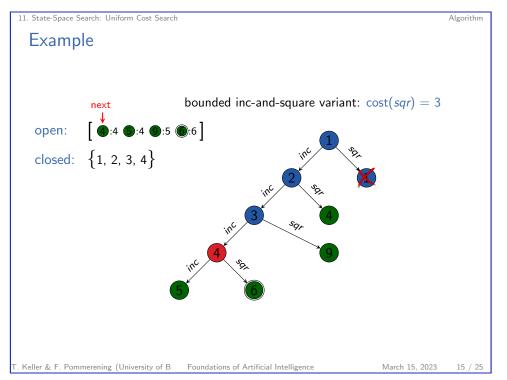


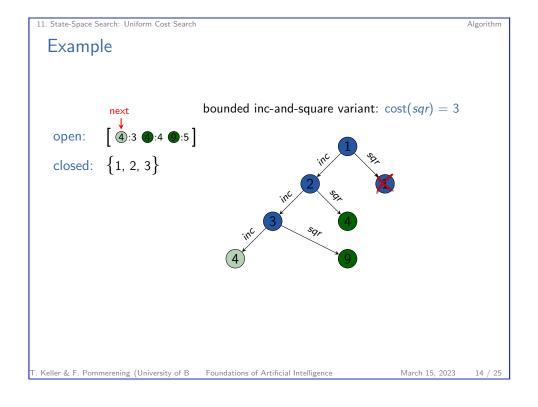
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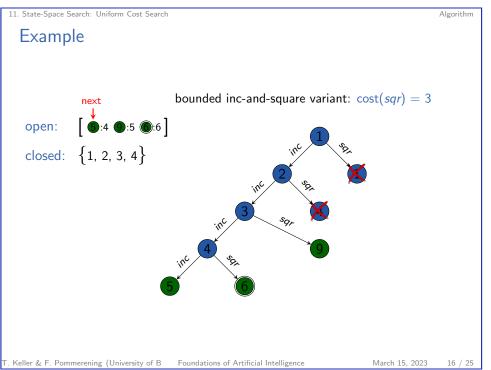
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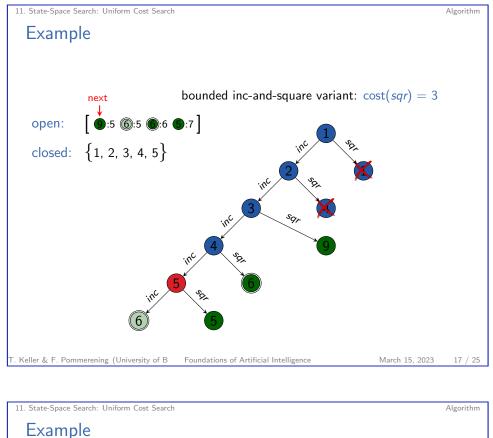


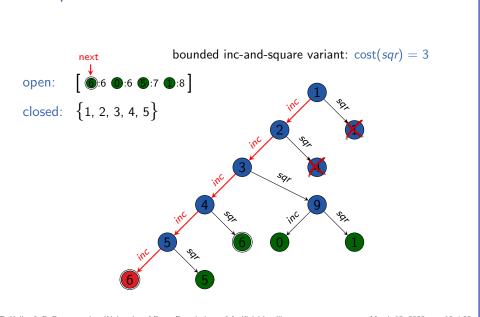


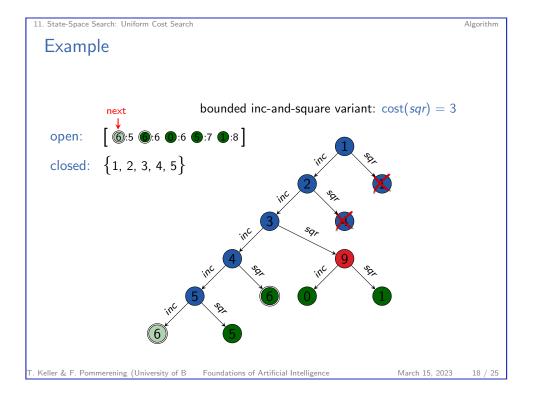


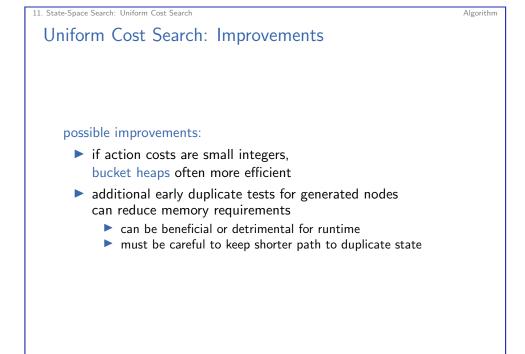












Properties

# 11.3 Properties

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11. State-Space Search: Uniform Cost Search Time and Space Complexity

properties of uniform cost search:

- Time complexity depends on distribution of action costs (no simple and accurate bounds).
  - Let  $\varepsilon := \min_{a \in A} cost(a)$  and consider the case  $\varepsilon > 0$ .
  - Let  $c^*$  be the optimal solution cost.
  - Let *b* be the branching factor and consider the case  $b \ge 2$ .
  - Then the time complexity is at most  $O(b^{\lfloor c^*/\varepsilon \rfloor + 1})$ . (Why?)
  - often a very weak upper bound
- space complexity = time complexity

# Completeness and Optimality

11. State-Space Search: Uniform Cost Search

### properties of uniform cost search:

- uniform cost search is complete (Why?)
- uniform cost search is optimal (Why?)

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Properties



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Properties

Summary

## Summary

uniform cost search: expand nodes in order of ascending path costs

- usually as a graph search
- then corresponds to Dijkstra's algorithm
- complete and optimal

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