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9. State-Space Search: Tree Search and Graph Search

Introduction

9.1 Introduction

9. State-Space Search: Tree Search and Graph Search

Search Algorithms

General Search Algorithm

iteratively create a search tree:

- starting with the initial state,
- repeatedly expand a state by generating its successors (which state depends on the used search algorithm)
- stop when a goal state is expanded (sometimes: generated)
- or all reachable states have been considered

In this chapter, we study two essential classes of search algorithms:

- tree search and
- ► graph search

(Each class consists of a large number of concrete algorithms.)

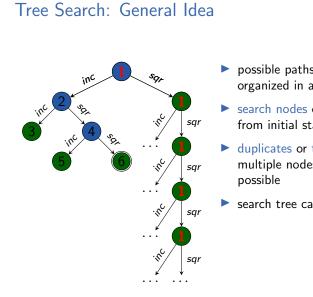
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Tree Search

Introduction

9. State-Space Search: Tree Search and Graph Search



- possible paths to be explored organized in a tree (search tree)
- search nodes correspond 1:1 to paths from initial state
- duplicates or transpositions (i.e., multiple nodes with identical state) possible
- search tree can have unbounded depth

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9.2 Tree Search

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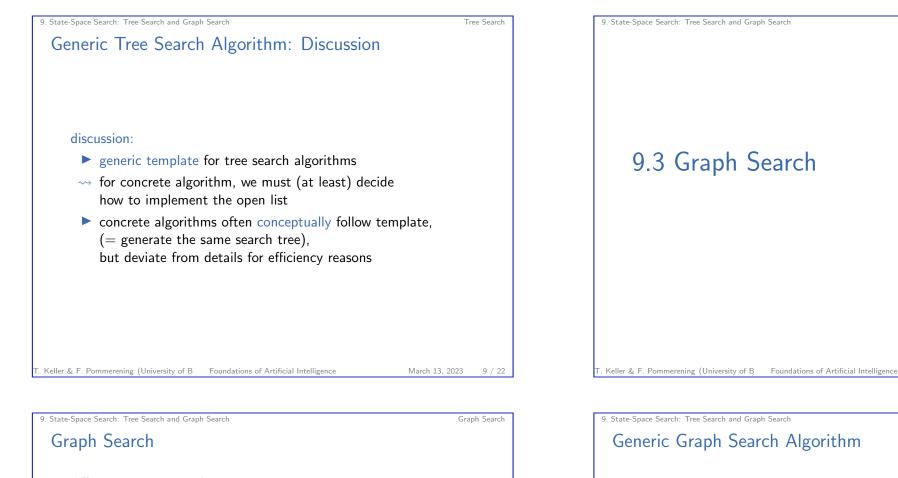
Tree Search

Tree Search

9. State-Space Search: Tree Search and Graph Search Generic Tree Search Algorithm

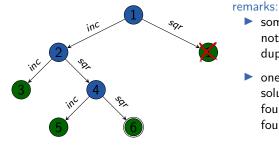
Generic Tree Search Algorithm open := new OpenList $open.insert(make_root_node())$ while not $open.is_empty()$: n := open.pop()if is_goal(n.state): return extract_path(n) for each $\langle a, s' \rangle \in succ(n.state)$: $n' := make_node(n, a, s')$ open.insert(n')return unsolvable

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differences to tree search:

- recognize duplicates: when a state is reached on multiple paths, only keep one search node
- search nodes correspond 1:1 to reachable states
- depth of search tree bounded



arks:

- some graph search algorithms do not immediately eliminate all duplicates (~> later)
- one possible reason: find optimal solutions when a path to state s found later is cheaper than one found earlier

open.insert(n')

if *closed*.lookup(*n*.state) = **none**:

return extract_path(n) for each $\langle a, s' \rangle \in \text{succ}(n.\text{state})$:

 $n' := make_node(n, a, s')$

Generic Graph Search Algorithm

closed.insert(n)

if is_goal(*n*.state):

open.insert(make_root_node())

open := **new** OpenList

return unsolvable

closed := **new** ClosedList

while not open.is_empty():
n := open.pop()

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Graph Search

Graph Search



9. State-Space Search: Tree Search and Graph Search

Evaluating Search Algorithms

Criteria: Time Complexity

four criteria for evaluating search algorithms:

Time Complexity

How much time does the algorithm need until termination?

- usually worst case analysis
- usually measured in generated nodes

often a function of the following quantities:

- b: (branching factor) of state space (max. number of successors of a state)
- ► *d*: search depth (length of longest path in generated search tree)

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Evaluating Search Algorithms

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Generic Tree Search Algorithm

- Is it complete? Is it semi-complete?
- ▶ Is it optimal?
- ▶ What is its worst-case time complexity?
- What is its worst-case space complexity?

Generic Graph Search Algorithm

- ▶ Is it complete? Is it semi-complete?
- ▶ Is it optimal?
- What is its worst-case time complexity?
- What is its worst-case space complexity?



Criteria: Space Complexity

four criteria for evaluating search algorithms:

Space Complexity

How much memory does the algorithm use?

- usually worst case analysis
- usually measured in (concurrently) stored nodes

often a function of the following quantities:

- **b**: (branching factor) of state space (max. number of successors of a state)
- ► *d*: search depth (length of longest path in generated search tree)

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