Foundations of Artificial Intelligence

6. State-Space Search: Representation of State Spaces

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State-Space Search: Overview

Chapter overview: state-space search

- 5.–7. Foundations
 - 5. State Spaces
 - 6. Representation of State Spaces
 - 7. Examples of State Spaces
- 8.–12. Basic Algorithms
- 13.–19. Heuristic Algorithms

Representation of State Spaces

Representation of State Spaces

- practically interesting state spaces are often huge $(10^{10}, 10^{20}, 10^{100} \text{ states})$
- How do we represent them, so that we can efficiently deal with them algorithmically?

three main options:

Representation

- as explicit (directed) graphs
- with declarative representations
- as a black box

Explicit Graphs

State Spaces as Explicit Graphs

State Spaces as Explicit Graphs

represent state spaces as explicit directed graphs:

- vertices = states
 - directed arcs = transitions
- → represented as adjacency list or adjacency matrix

Example (explicit graph for bounded inc-and-square)

ai06-bounded-inc-and-square.graph

State Spaces as Explicit Graphs

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- vertices = states
- directed arcs = transitions

→ represented as adjacency list or adjacency matrix

Example (explicit graph for 8-puzzle)

ai06-puzzle8.graph

State Spaces as Explicit Graphs: Discussion

discussion:

- impossible for large state spaces (too much space required)
- if spaces small enough for explicit representations, solutions easy to compute: Dijkstra's algorithm $O(|S| \log |S| + |T|)$
- interesting for time-critical all-pairs-shortest-path queries (examples: route planning, path planning in video games)

Declarative Representations

Declarative Representations

State Spaces with Declarative Representations

State Spaces with Declarative Representations

represent state spaces declaratively:

- compact description of state space as input to algorithms → state spaces exponentially larger than the input
- algorithms directly operate on compact description
- → allows automatic reasoning about problem: reformulation, simplification, abstraction, etc.

Example (declarative representation for 8-puzzle)

puzzle8-domain.pddl + puzzle8-problem.pddl

Black Box

State Spaces as Black Boxes

State Spaces as Black Boxes

Define an abstract interface for state spaces.

For state space $S = \langle S, A, cost, T, s_I, S_{\star} \rangle$ we need these methods:

- init(): generate initial state result: state s₁
- is_goal(s): test if s is a goal state result: **true** if $s \in S_+$; **false** otherwise
- succ(s): generate applicable actions and successors of s result: sequence of pairs $\langle a, s' \rangle$ with $s \xrightarrow{a} s'$
- cost(a): gives cost of action a result: $cost(a) \ (\in \mathbb{N}_0)$

remark: we extend the interface later in a small but important way

State Spaces as Black Boxes: Example and Discussion

Example (Black Box Representation for 8-Puzzle)

demo: puzzle8.py

- in the following: focus on black box model
- explicit graphs only as illustrating examples
- near end of semester: declarative state spaces (classical planning)

Summary

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Summary

- state spaces often huge ($> 10^{10}$ states) → how to represent?
- explicit graphs: adjacency lists or matrices; only suitable for small problems
- declaratively: compact description as input to search algorithms
- black box: implement an abstract interface