

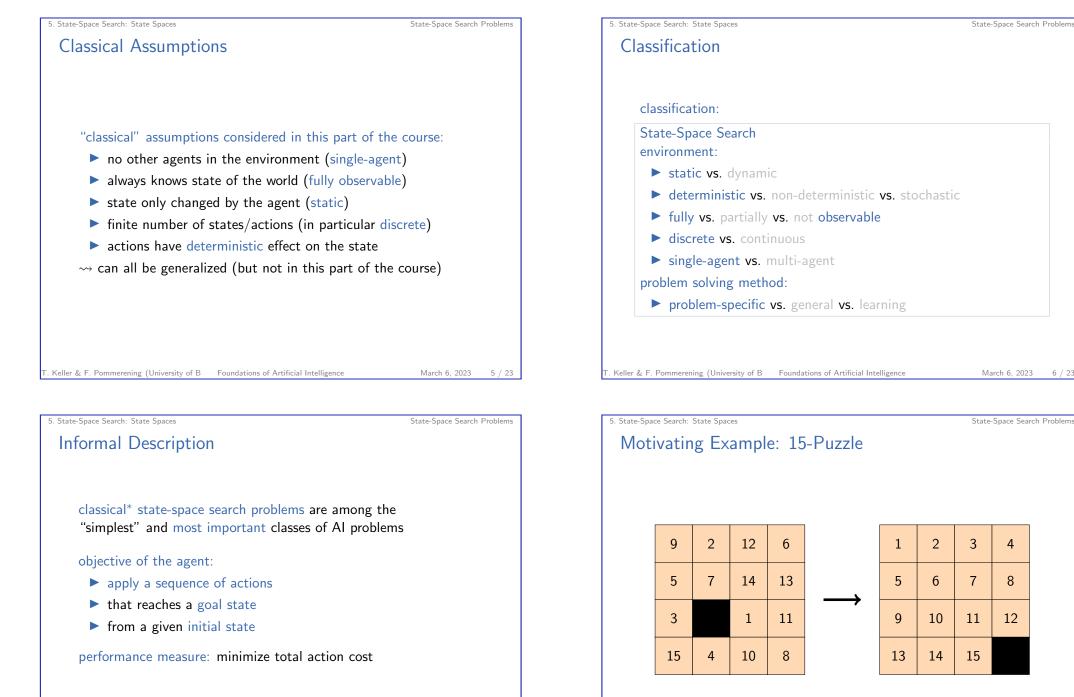
5. State-Space Search: State Spaces

State-Space Search Problems

## 5.1 State-Space Search Problems

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5.1 State-Space Search Problems		
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(for simplicity, we omit "classical" in the following)

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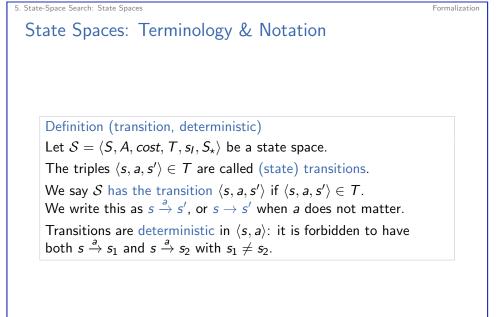
State Spaces

To cleanly study search problems we need a formal model.

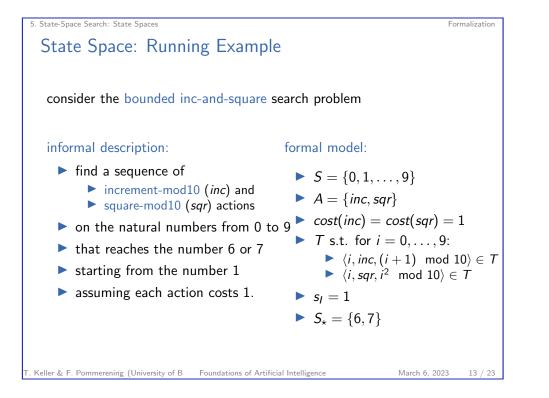
Definition (state space) A state space or transition system is a 6-tuple  $S = \langle S, A, cost, T, s_l, S_{\star} \rangle$  with ► finite set of states S ▶ finite set of actions A ▶ action costs *cost* :  $A \to \mathbb{R}^+_0$ **•** transition relation  $T \subseteq S \times A \times S$  that is deterministic in  $\langle s, a \rangle$  (see next slide) • initial state  $s_l \in S$ ▶ set of goal states  $S_{+} \subset S$ 

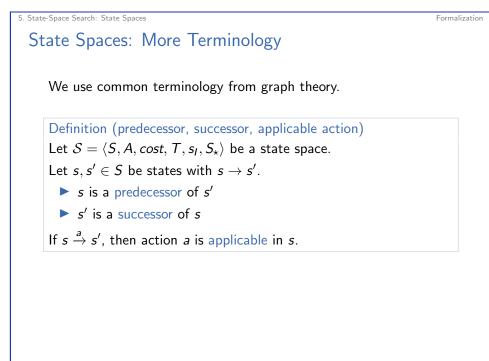


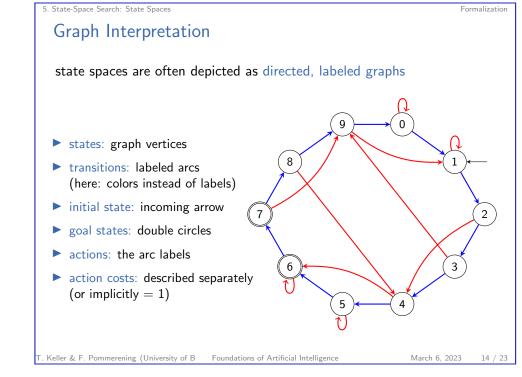
5. State-Space Search: State Spaces

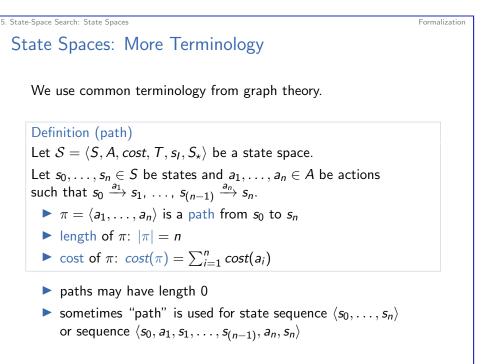


Formalization







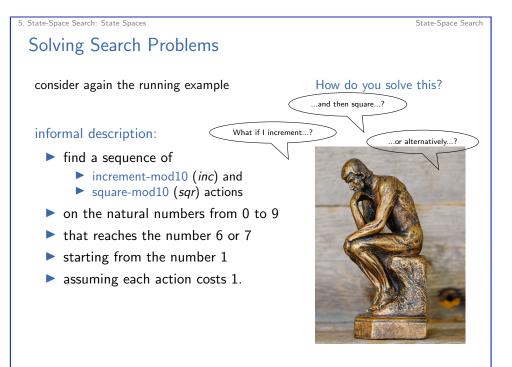




## State Spaces: More Terminology

more terminology:

Definition (reachable, solution, optimal)
Let S = ⟨S, A, cost, T, s<sub>I</sub>, S<sub>\*</sub>⟩ be a state space.
state s is reachable if a path from s<sub>I</sub> to s exists
paths from s ∈ S to some state s<sub>\*</sub> ∈ S<sub>\*</sub> are solutions for/from s
solutions for s<sub>I</sub> are called solutions for S
optimal solutions (for s) have minimal costs among all solutions (for s)



5.3 State-Space Search

## State-Space Search

5. State-Space Search: State Spaces

State-Space Search

5. State-Space Search: State Spaces

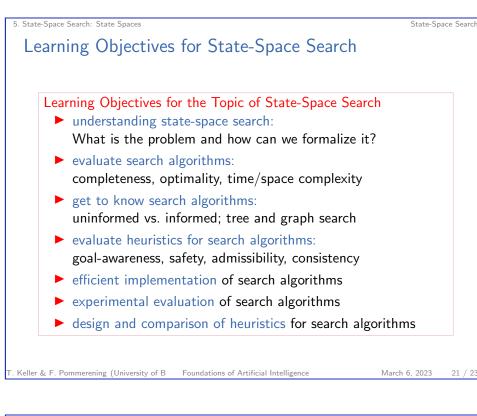
State-space search is the algorithmic problem of finding solutions in state spaces or proving that no solution exists.

In optimal state-space search, only optimal solutions may be returned.

Formalization

State-Space Search

State-Space Search



21 / 23 5. State-Space Search: State Spaces Summary Summary classical state-space search problems: find action sequence from initial state to a goal state performance measure: sum of action costs ► formalization via state spaces: states, actions, action costs, transitions, initial state, goal states terminology for transitions, paths, solutions definition of (optimal) state-space search Keller & F. Pommerening (University of B Foundations of Artificial Intelligence March 6, 2023 23 / 23

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