Foundations of Artificial Intelligence

11. State-Space Search: Uniform Cost Search

Malte Helmert and Thomas Keller

University of Basel

March 16, 2020

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

Foundations of Artificial Intelligence

March 16, 2020 — 11. State-Space Search: Uniform Cost Search

- 11.1 Introduction
- 11.2 Algorithm
- 11.3 Properties
- 11.4 Summary

Foundations of Artificial Intelligence

March 16, 2020 2 / 15

State-Space Search: Overview

Chapter overview: state-space search

- ▶ 5.–7. Foundations
- ▶ 8.–12. Basic Algorithms
 - ▶ 8. Data Structures for Search Algorithms
 - ▶ 9. Tree Search and Graph Search
 - ▶ 10. Breadth-first Search
 - ▶ 11. Uniform Cost Search
 - ▶ 12. Depth-first Search and Iterative Deepening
- ▶ 13.–19. Heuristic Algorithms

11. State-Space Search: Uniform Cost Search

11.1 Introduction

M. Helmert, T. Keller (University of Basel) Foundations of Artificial Intelligence

March 16, 2020

M. Helmert, T. Keller (University of Basel) Foundations of Artificial Intelligence

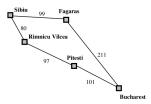
March 16, 2020

11. State-Space Search: Uniform Cost Search

Introduction

Uniform Cost Search

- breadth-first search optimal if all action costs equal
- ▶ otherwise no optimality guarantee → example:



remedy: uniform cost search

- ▶ always expand a node with minimal path cost $(n.path_cost a.k.a. g(n))$
- ▶ implementation: priority queue (min-heap) for open list

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

5 / 1

11. State-Space Search: Uniform Cost Search

11.2 Algorithm

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

6 / 15

11. State-Space Search: Uniform Cost Search

M. Helmert, T. Keller (University of Basel)

Algorithm

Reminder: Generic Graph Search Algorithm

reminder from Chapter 9:

```
Generic Graph Search

open := new \text{ OpenList}

open.insert(make\_root\_node())

closed := new \text{ ClosedList}

while not open.is\_empty():

n := open.pop()

if closed.lookup(n.state) = none:

closed.insert(n)

if is\_goal(n.state):

return \text{ extract\_path}(n)

for each \langle a, s' \rangle \in succ(n.state):

n' := make\_node(n, a, s')

open.insert(n')

return unsolvable
```

```
11. State-Space Search: Uniform Cost Search
 Uniform Cost Search
     Uniform Cost Search
     open := new MinHeap ordered by g
     open.insert(make_root_node())
     closed := new HashSet
     while not open.is_empty():
          n := open.pop_min()
          if n.state ∉ closed:
                closed.insert(n)
                if is_goal(n.state):
                     return extract_path(n)
               for each \langle a, s' \rangle \in \text{succ}(n.\text{state}):
                     n' := \mathsf{make\_node}(n, a, s')
                     open.insert(n')
     return unsolvable
```

Foundations of Artificial Intelligence

March 16, 2020

0 7

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

20 8 / 1

11. State-Space Search: Uniform Cost Search

Uniform Cost Search: Discussion

Adapting generic graph search to uniform cost search:

- ▶ here, early goal tests/early updates of the closed list not a good idea. (Why not?)
- ▶ as in BFS-Graph, a set is sufficient for the closed list
- ▶ a tree search variant is possible, but rare: has the same disadvantages as BFS-Tree and in general not even semi-complete (Why not?)

Remarks:

- ▶ identical to Dijkstra's algorithm for shortest paths
- ▶ for both: variants with/without delayed duplicate elimination

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

11. State-Space Search: Uniform Cost Search

11.3 Properties

11. State-Space Search: Uniform Cost Search

Uniform Cost Search: Improvements

possible improvements:

- ▶ if action costs are small integers, bucket heaps often more efficient
- ▶ additional early duplicate tests for generated nodes can reduce memory requirements
 - can be beneficial or detrimental for runtime
 - must be careful to keep shorter path to duplicate state

11. State-Space Search: Uniform Cost Search

Completeness and Optimality

properties of uniform cost search:

- uniform cost search is complete (Why?)
- uniform cost search is optimal (Why?)

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

11. State-Space Search: Uniform Cost Search

Properties

Time and Space Complexity

properties of uniform cost search:

- ► Time complexity depends on distribution of action costs (no simple and accurate bounds).
 - ▶ Let $\varepsilon := \min_{a \in A} cost(a)$ and consider the case $\varepsilon > 0$.
 - ightharpoonup Let c^* be the optimal solution cost.
 - Let b be the branching factor and consider the case $b \ge 2$.
 - ► Then the time complexity is at most $O(b^{\lfloor c^*/\varepsilon \rfloor + 1})$. (Why?)
 - often a very weak upper bound
- space complexity = time complexity

M. Helmert, T. Keller (University of Basel)

Foundations of Artificial Intelligence

March 16, 2020

6, 2020 13 /

11. State-Space Search: Uniform Cost Search

Summar

Summary

uniform cost search: expand nodes in order of ascending path costs

- usually as a graph search
- ▶ then corresponds to Dijkstra's algorithm
- complete and optimal

M. Helmert, T. Keller (University of Basel) Foundations of Artificial Intelligence

March 16, 2020

15 / 15

11.4 Summary

March 16, 2020

M. Helmert, T. Keller (University of Basel) Foundations of Artificial Intelligence