### Foundations of Artificial Intelligence

37. Automated Planning: Abstraction and Pattern Databases

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May 13, 2016

#### Planning Heuristics

We consider three basic ideas for general heuristics:

- Delete Relaxation
- Abstraction → this and next chapter
- Landmarks

#### Planning Heuristics

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- Delete Relaxation
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#### Abstraction: Idea

Estimate solution costs by considering a smaller planning task.

#### Automated Planning: Overview

#### Chapter overview: planning

- 33. Introduction
- 34. Planning Formalisms
- 35.–36. Planning Heuristics: Delete Relaxation
- 37.–38. Planning Heuristics: Abstraction
  - 37. Abstraction and Pattern Databases
  - 38. Merge-and-Shrink-Abstractions
- 39.–40. Planning Heuristics: Landmarks

# $\mathsf{SAS}^+$

# SAS<sup>+</sup> Encoding

- in this and the next chapter: SAS<sup>+</sup> encoding instead of STRIPS (see Chapter 34)
- difference: state variables v not binary, but with finite domain dom(v)
- accordingly, preconditions, effects, goals specified as partial assignments
- everything else equal to STRIPS

(In practice, planning systems convert automatically between STRIPS and SAS<sup>+</sup>.)

### SAS<sup>+</sup> Planning Task

#### Definition (SAS<sup>+</sup> planning task)

A SAS<sup>+</sup> planning task is a 5-tuple  $\Pi = \langle V, dom, I, G, A \rangle$ with the following components:

- V: finite set of state variables
- dom: domain; dom(v) finite and non-empty for all  $v \in V$ 
  - states: total assignments for V according to dom
- I: the initial state (state = total assignment)
- G: goals (partial assignment)
- A: finite set of actions a with
  - pre(a): its preconditions (partial assignment)
  - eff(a): its effects (partial assignment)
  - $cost(a) \in \mathbb{N}_0$ : its cost

German: SAS<sup>+</sup>-Planungsaufgabe

## State Space of SAS<sup>+</sup> Planning Task

#### Definition (state space induced by SAS<sup>+</sup> planning task)

Let  $\Pi = \langle V, \text{dom}, I, G, A \rangle$  be a SAS<sup>+</sup> planning task.

Then  $\Pi$  induces the state space  $S(\Pi) = \langle S, A, cost, T, s_0, S_{\star} \rangle$ :

- set of states: total assignments of V according to dom
- actions: actions A defined as in Π
- action costs: cost as defined in Π
- transitions:  $s \xrightarrow{a} s'$  for states s, s' and action a iff
  - pre(a) complies with s (precondition satisfied)
  - s' complies with eff(a) for all variables mentioned in eff; complies with s for all other variables (effects are applied)
- initial state:  $s_0 = I$
- goal states:  $s \in S_{\star}$  for state s iff G complies with s

German: durch SAS<sup>+</sup>-Planungsaufgabe induzierter Zustandsraum

### Example: Logistics Task with One Package, Two Trucks

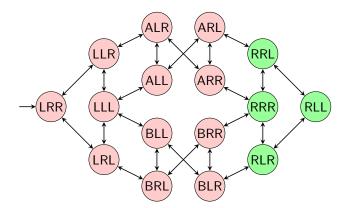
#### Example (one package, two trucks)

Consider the SAS<sup>+</sup> planning task  $\langle V, dom, I, G, A \rangle$  with:

- $V = \{p, t_A, t_B\}$
- $dom(p) = \{L, R, A, B\}$  and  $dom(t_A) = dom(t_B) = \{L, R\}$
- $I = \{p \mapsto L, t_A \mapsto R, t_B \mapsto R\}$  and  $G = \{p \mapsto R\}$
- $A = \{pickup_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$   $\cup \{drop_{i,j} \mid i \in \{A, B\}, j \in \{L, R\}\}$   $\cup \{move_{i,j,j'} \mid i \in \{A, B\}, j, j' \in \{L, R\}, j \neq j'\}$  with:
  - $pickup_{i,j}$  has preconditions  $\{t_i \mapsto j, p \mapsto j\}$ , effects  $\{p \mapsto i\}$
  - $drop_{i,j}$  has preconditions  $\{t_i \mapsto j, p \mapsto i\}$ , effects  $\{p \mapsto j\}$
  - $move_{i,j,j'}$  has preconditions  $\{t_i \mapsto j\}$ , effects  $\{t_i \mapsto j'\}$
  - All actions have cost 1.

pickup corresponds to load, and drop to unload from Chapter 35 (renamed to avoid confusion in the following abbreviations)

### State Space for Example Task



- state  $\{p \mapsto i, t_A \mapsto j, t_B \mapsto k\}$  denoted as ijk
- annotations of edges not shown for simplicity
- for example, edge from LLL to ALL has annotation pickupALL

# **Abstractions**

### State Space Abstraction

State space abstractions drop distinctions between certain states, but preserve the state space behavior as well as possible.

- An abstraction of a state space  $\mathcal S$  is defined by an abstraction function  $\alpha$  that determines which states can be distinguished in the abstraction.
- Based on S and  $\alpha$ , we compute the abstract state space  $S^{\alpha}$  which is "similar" to S but smaller.

German: Abstraktionsfunktion, abstrakter Zustandsraum

#### Abstraction Heuristic

Use abstract goal distances (goal distances in  $\mathcal{S}^{\alpha}$ ) as heuristic values for concrete goal distances (goal distances in  $\mathcal{S}$ ).  $\rightarrow$  abstraction heuristic  $h^{\alpha}$ 

German: abstrakte/konkrete Zielabstände, Abstraktionsheuristik

#### Induced Abstraction

#### Definition (induced abstraction)

Let  $S = \langle S, A, cost, T, s_0, S_{\star} \rangle$  be a state space, and let  $\alpha: S \to S'$  be a surjective function.

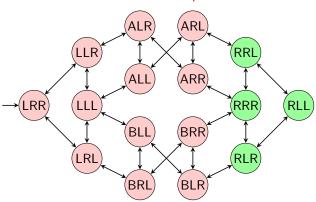
The abstraction of S induced by  $\alpha$ , denoted as  $S^{\alpha}$ . is the state space  $S^{\alpha} = \langle S', A, \cos t, T', s'_0, S'_{\star} \rangle$  with:

- $T' = \{ \langle \alpha(s), a, \alpha(t) \rangle \mid \langle s, a, t \rangle \in T \}$
- $s_0' = \alpha(s_0)$
- $S'_{+} = \{ \alpha(s) \mid s \in S_{+} \}$

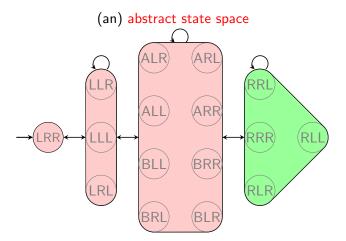
German: induzierte Abstraktion

#### Abstraction: Example

#### concrete state space

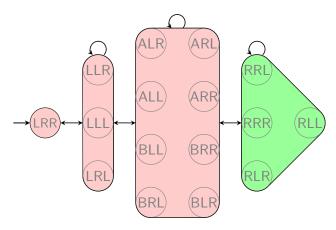


#### Abstraction: Example



remark: Most edges correspond to several (parallel) transitions with different annotations.

#### Abstraction Heuristic: Example

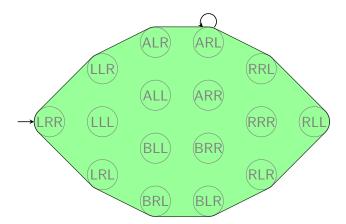


$$h^{\alpha}(\{p\mapsto \mathsf{L},t_{\mathsf{A}}\mapsto \mathsf{R},t_{\mathsf{B}}\mapsto \mathsf{R}\})=3$$

#### Abstraction Heuristics: Discussion

- Every abstraction heuristic is admissible and consistent. (proof idea?)
- The choice of the abstraction function  $\alpha$  is very important.
  - Every  $\alpha$  yields an admissible and consistent heuristic.
  - But most  $\alpha$  lead to poor heuristics.
- An effective  $\alpha$  must yield an informative heuristic . . .
- ... as well as being efficiently computable.
- How to find a suitable  $\alpha$ ?

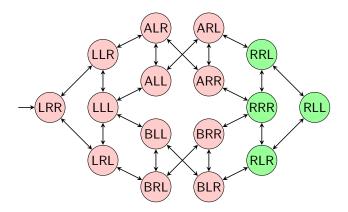
### Usually a Bad Idea: Single-State Abstraction



#### one state abstraction: $\alpha(s) := \text{const}$

- + compactly representable and  $\alpha$  easy to compute
- very uninformed heuristic

### Usually a Bad Idea: Identity Abstraction



identity abstraction:  $\alpha(s) := s$ 

- + perfect heuristic and  $\alpha$  easy to compute
- too many abstract states  $\rightsquigarrow$  computation of  $h^{\alpha}$  too hard

### Automatic Computation of Suitable Abstractions

#### Main Problem with Abstraction Heuristics

How to find a good abstraction?

We introduce two successful methods:

- pattern databases (PDBs) (Culberson & Schaeffer, 1996)
- merge-and-shrink abstractions (Dräger, Finkbeiner & Podelski, 2006)

German: Musterdatenbanken, Merge-and-Shrink-Abstraktionen

Pattern Databases •0000000

# Pattern Databases

#### Pattern Databases: Background

- The most common abstraction heuristics are pattern database heuristics.
- originally introduced for the 15-puzzle (Culberson & Schaeffer, 1996) and for Rubik's Cube (Korf, 1997)
- introduced for automated planning by Edelkamp (2001)

Pattern Databases

- for many search problems the best known heuristics
- many many research papers studying
  - theoretical properties
  - efficient implementation and application
  - pattern selection
  - . . .

#### Pattern Databases: Projections

A PDB heuristic for a planning task is an abstraction heuristic where

Pattern Databases

- some aspects (= state variables) of the task are preserved with perfect precision while
- all other aspects are not preserved at all.

formalized as projections; example:

- $s = \{v_1 \mapsto d_1, v_2 \mapsto d_2, v_3 \mapsto d_3\}$
- projection on  $P = \{v_1\}$  (= ignore  $v_2, v_3$ ):  $\alpha(s) = s|_P = \{v_1 \mapsto d_1\}$
- projection on  $P = \{v_1, v_3\}$  (= ignore  $v_2$ ):  $\alpha(s) = s|_{P} = \{v_1 \mapsto d_1, v_3 \mapsto d_3\}$

German: Projektionen

#### Pattern Databases: Definition

#### Definition (pattern database heuristic)

Let P be a subset of the variables of a planning task.

The abstraction heuristic induced by the projection  $\pi_P$  on P is called pattern database heuristic (PDB heuristic) with pattern P.

Pattern Databases

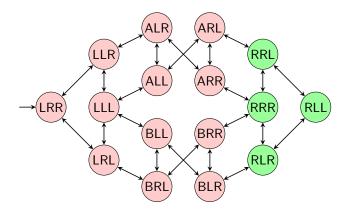
abbreviated notation:  $h^P$  for  $h^{\pi_P}$ 

German: Musterdatenbank-Heuristik

#### remark:

"pattern databases" in analogy to endgame databases (which have been successfully applied in 2-person-games)

### Example: Concrete State Space



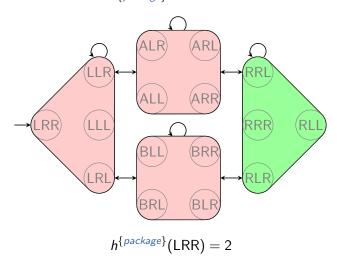
Pattern Databases 00000000

- state variable *package*: {L, R, A, B}
- state variable *truck A*: {L, R}
- state variable *truck B*: {L, R}

Pattern Databases

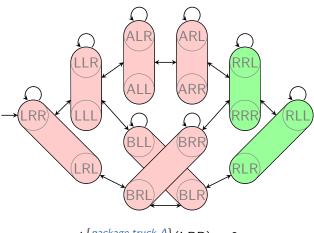
## Example: Projection (1)

#### abstraction induced by $\pi_{\{package\}}$ :



## Example: Projection (2)

### abstraction induced by $\pi_{\{package,truck\ A\}}$ :

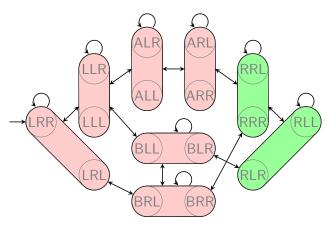


Pattern Databases 00000000

$$h^{\{package,truck\ A\}}(LRR) = 2$$

### Example: Projection (2)

#### abstraction induced by $\pi_{\{package,truck\ A\}}$ :



Pattern Databases 00000000

$$\mathit{h}^{\{\mathit{package},\mathit{truck}\ A\}}(\mathsf{LRR}) = 2$$

#### Pattern Databases in Practice

practical aspects which we do not discuss in detail:

- How to automatically find good patterns?
- How to combine multiple PDB heuristics?
- How to implement PDB heuristics efficiently?
  - good implementations efficiently handle abstract state spaces with 107, 108 or more abstract states
  - effort independent of the size of the concrete state space
  - usually all heuristic values are precomputed
    - → space complexity = number of abstract states

# Summary

#### Summary

- basic idea of abstraction heuristics: estimate solution cost by considering a smaller planning task.
- formally: abstraction function  $\alpha$  maps states to abstract states and thus defines which states can be distinguished by the resulting heuristic.
- induces abstract state space whose solution costs are used as heuristic
- Pattern database heuristics are abstraction heuristics. based on projections onto state variable subsets (patterns): states are distinguishable if they differ on the pattern.